

## Ramblings from Hao

# C Language Implementation for Proportional-Resonant Controller

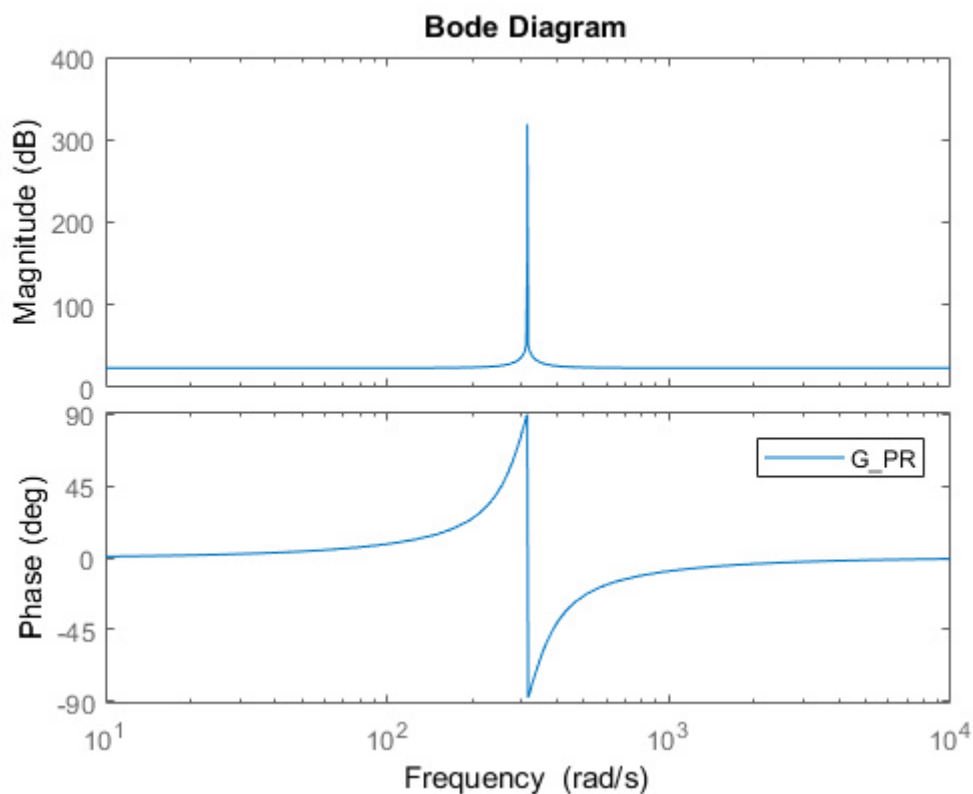
📅 2018-06-22 | 📅 2020-02-09 | 📁 Control | 💬 0 Comments

## 1. Introduction to Proportional-Resonant Controller

First, let's see the transfer function of PR controller and its bode diagram :

$$G_{PR}(s) = K_p + \frac{K_r s}{s^2 + \omega_r^2}$$

where the  $\omega_r$  is the resonant frequency.



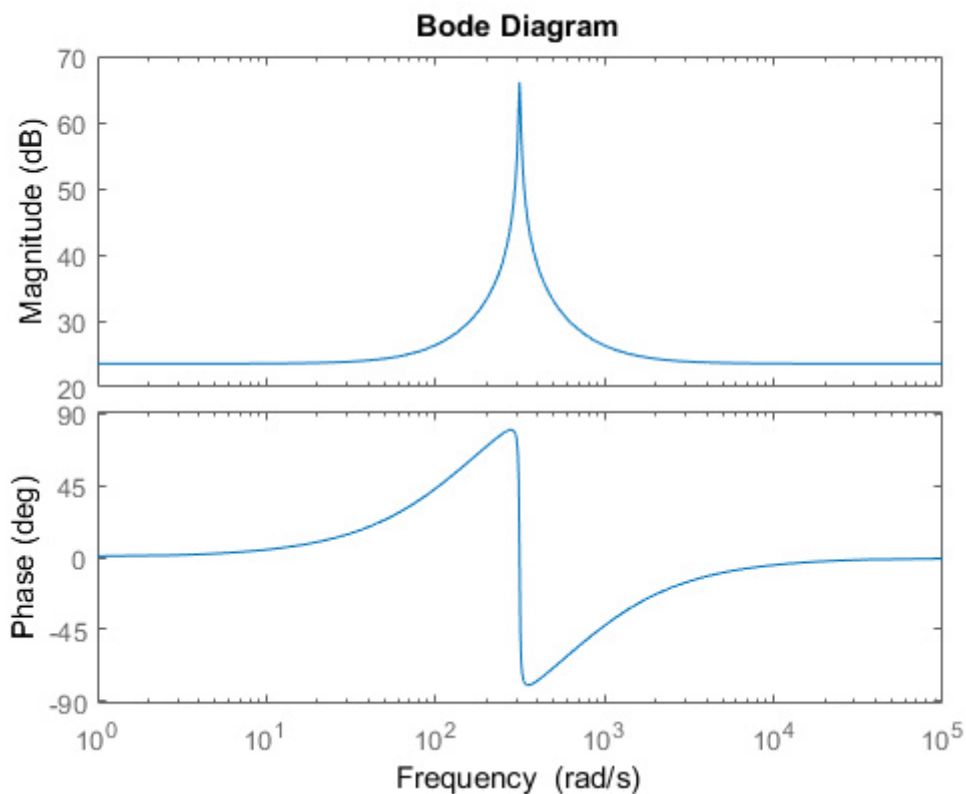
Bode diagram of PR Controller

As can be seen in the bode diagram, the gain at 50Hz (314 rad/s) is infinite, so PR controller can be used to track reference of specific frequency. However, the reference frequency is not always a constant, e.g. the frequency of electricity grid. In practice, Quasi-Proportional-Resonant can be used to solve this problem.

The transfer function of QPR and its bode diagram:

$$G_{QPR}(s) = K_p + \frac{2\omega_i K_r s}{s^2 + 2\omega_i s + \omega_r^2}$$

where the addition of  $2\omega_r$  reduces the gain at resonant frequency but increase the band width around resonant frequency.



Bode diagram of QPR Controller

You can change the parameter  $\omega_r$  and run the demo code below to see how it changes the shape of bode diagram.

```
1  s = tf([1, 0], 1) ;
2
3  Kp = 15 ;
4  Kr = 2000 ;
5  wr = 50 * 2 * pi ;
```

```

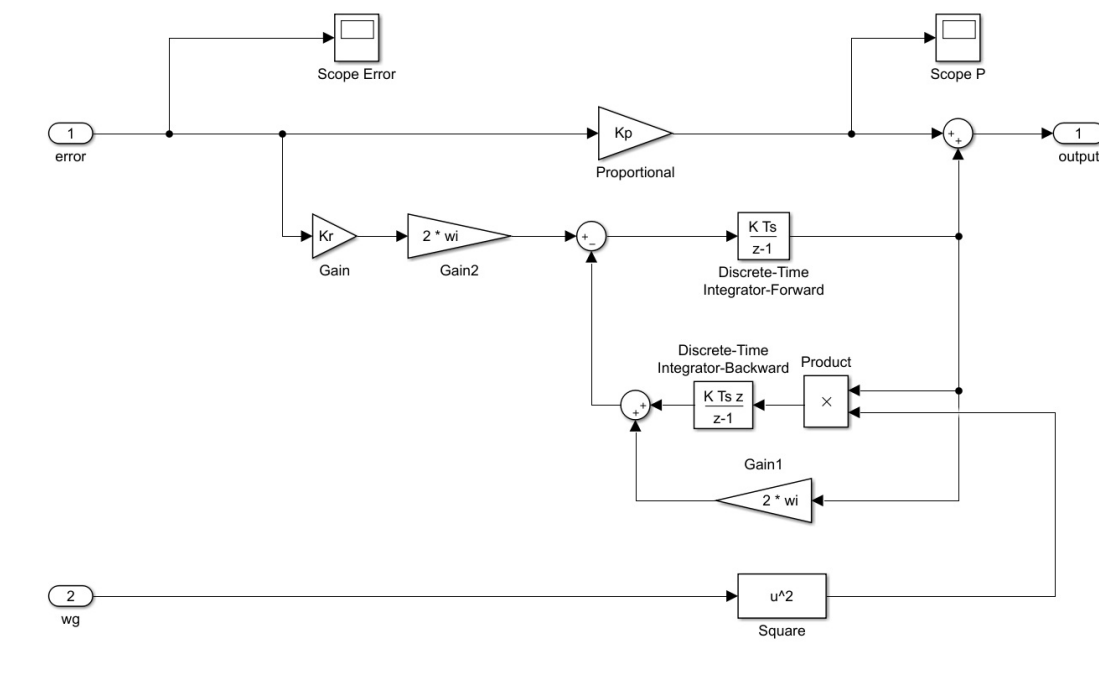
6  wi = pi ;
7
8  G_PR = Kp + Kr * s / (s^2 + wr^2)
9  figure
10 bode(G_PR)
11
12 G_QPR = Kp + 2 * wi * Kr * s / (s^2 + 2 * wi * s + wr^2)
13 figure
14 bode(G_QPR)

```

## 2. C Language Implementation

The code is in the repository [Controller](#), feel free to use it for your own application.

The structure of QPR controller implemented is as below:



### PR Implementation

As shown in [Effects of Discretization Methods on the Performance of Resonant Controllers](#), the structure of QPR controller can be implemented using 2 integrators.

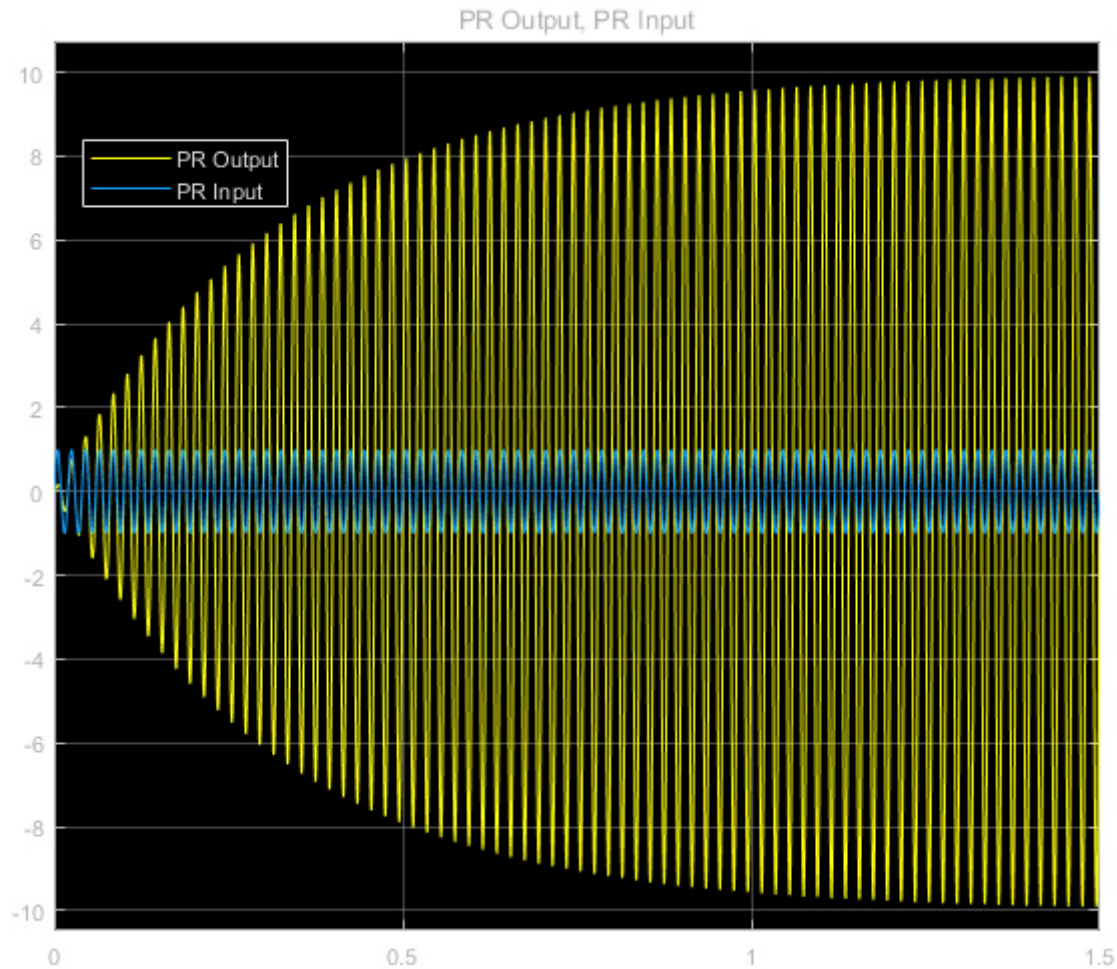
The implemented structure above has 2 advantages:

- Easy to implemented, 2 integrators used.
- Autonomous resonant frequency adaption:  $\omega_r$  can be fed into the controller and real-time resonant frequency adaption is achieved.

You can run the [Simulink demo](#) to see the effectiveness of this structure

- $K_p$  is set to be 0 and  $K_r$  to be 10
- $\omega_i$  is set to be  $0.01\omega_r$

The simulation result is as below:



### Simulation Result

As you can see in the result above, the input signal is a sine wave with an amplitude of 1 and the output with an amplitude of 10, corresponding to the parameter--  $K_p$  is 0 and  $K_r$  is 10.

## 3. Reference

1. [Effects of Discretization Methods on the Performance of Resonant Controllers](#)

2. [百度文库文档](#)

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< 从伯德图(Bode Plot)说起

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